

# Toward a Formalism for Conservative Claims about the Dependability of Software-Based Systems

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**Abstract**—In recent work, we have argued for a formal treatment of confidence about the claims made in dependability cases for software-based systems. The key idea underlying this work is “the inevitability of uncertainty”: It is rarely possible to assert that a claim about safety or reliability is true with certainty. Much of this uncertainty is *epistemic* in nature, so it seems inevitable that expert judgment will continue to play an important role in dependability cases. Here, we consider a simple case where an expert makes a claim about the probability of failure on demand (*pdf*) of a subsystem of a wider system and is able to express his confidence about that claim probabilistically. An important, but difficult, problem then is how such subsystem (claim, confidence) pairs can be propagated through a dependability case for a wider system, of which the subsystems are components. An informal way forward is to justify, at high confidence, a strong claim, and then, conservatively, only claim something much weaker: “I’m 99 percent confident that the *pdf* is less than  $10^{-5}$ , so it’s reasonable to be 100 percent confident that it is less than  $10^{-3}$ .” These conservative *pdfs* of subsystems can then be propagated simply through the dependability case of the wider system. In this paper, we provide formal support for such reasoning.

**Index Terms**—Bayesian probability, safety case, software reliability.



## 1 INTRODUCTION

THERE is now a huge literature on the assessment of the dependability of software-based systems, going back several decades. In recent years, the assessment process has started to be formalized in *dependability cases*, most notably safety cases (see, for example, [1], [2], [3], [4], [5]). There are now safety standards that require safety cases, e.g., [6], [7].

In this paper, we shall discuss some problems arising from the need to assess *uncertainty* in cases where dependability claims about a software component form part of a wider *system* case. We believe that some aspects of uncertainty have long been neglected or misjudged. For example, expert judgments about the impact of the “quality” of software development processes upon the dependability of software systems often underestimate the uncertainties involved. In recent work, we have proposed a formal quantitative treatment of “confidence” to address this omission [8], [9], [10].

Computer scientists, including software engineers, have long had an uneasy relationship with uncertainty and with its most powerful calculus, probability. Some of us can remember discussions of 30 years ago about software reliability. It was difficult then to persuade some software

experts that there was inherent uncertainty in the failure processes of programs and that *probability* was the appropriate way of capturing this uncertainty. Instead, it was asserted that software failed *systematically* and thus that probabilistic notions of “reliability” were meaningless.

Over the years, the position has changed. It is now widely agreed that “systematic failure” just means that a program that has failed in certain circumstances will *always* fail whenever those circumstances are exactly repeated. The uncertainty lies in our not knowing beforehand *which* circumstances (e.g., inputs to a program) will cause failure and *when* these will arise during the operational execution of the program. It is this uncertainty that is represented in a probabilistic measure of dependability, such as probability of failure on demand (*pdf*).

The uncertainty discussed above concerns system behavior—it is “uncertainty-in-the-world.” In the jargon, this is called aleatory uncertainty. There is another form of uncertainty that has, we believe, been neglected by the software engineering community: This is uncertainty in the dependability assessment process itself. This is called epistemic uncertainty, and it concerns uncertainty in our “beliefs-about-the-world” [11].

The presence of epistemic uncertainty means that we cannot be certain that a claim about dependability—e.g., the *pdf* is smaller than  $10^{-3}$ —is true. We might reasonably expect that by collecting more supportive evidence, we would increase our confidence in the truth of the claim, but it will rarely be possible to collect sufficient evidence to eliminate doubt completely.<sup>1</sup> This prompts questions such as: *How*

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1. One exception might be exhaustive testing in some specialized situations. Such exceptions are, we believe, very rare.

confident are we that the claim is true? How do we express “confidence” quantitatively? How do we incorporate this “assessment uncertainty” into wider dependability cases and into decision making?

Consider the simple example of operational testing of an on-demand software-based system. It is put on test and survives 4,602 demands without failure. It is a simple statistical exercise [12], [13] to show that you can claim the *pdf* is smaller than  $10^{-3}$  with 99 percent confidence (there is only a 0.01 probability that the *pdf* is greater than  $10^{-3}$ ). The assumptions here include: The oracle is perfect (i.e., it reports failure if and only if there truly is a failure), the test cases are generated in a way that accurately represents the operational environment (i.e., each is selected with the same probability as in operational use).

If the assumptions are correct in this example, the only epistemic uncertainty arises from the extensiveness of the evidence; if we were to see more failure-free demands, we would have greater than 99 percent confidence in the claim. When the only epistemic uncertainty is the extensiveness of the evidence, as here, it is easy to compute its impact upon confidence: For any particular number of failure-free demands, it is a simple matter to compute how much confidence we should have in the *pdf* claim of  $10^{-3}$ .

In practice, of course, the assessor would not be certain, the assumptions were true, and this extra epistemic uncertainty would reduce his confidence in the dependability claim. The impact of assumption doubt upon confidence in a claim is generally harder to quantify and likely to involve expert judgment. See [10] for a more complex example in which a Bayesian Belief Net is used to structure an argument involving different kinds of assumption doubt. There has been extensive research in recent years on methods for elicitation of expert beliefs to populate such arguments—see [14] for a recent survey—but this remains a difficult area.

The difficulties involved in incorporating software dependability assessment into quantitative safety cases for wider systems, of which the software can be regarded as a component, are well illustrated by the licensing process for the Sizewell B nuclear reactor in the UK in the early 1990s. There was extensive discussion—much of it in the public domain—about the reliability of the software in the primary protection system (PPS). The original reliability requirement for this system was a *pdf* no worse than  $10^{-4}$ . However, it soon became apparent that nuclear industry experts could not come to a consensus that the evidence (quality of production process, testing and static analysis of the delivered product, etc.) was strong enough to support the  $10^{-4}$  claim with sufficiently high confidence.

The safety system of Sizewell B comprises the software-based PPS and a simpler hardware secondary protection system (SPS) in a one-out-of-two architecture [15]. When the PPS claim turned out not to be supportable with sufficient confidence, an extensive review of the wider plant safety case was made, including what could be claimed for the SPS. This showed that the contribution of the overall safety system to the plant safety case would be satisfied if  $10^{-3}$  could be claimed for the PPS (partly because a stronger claim could be made for the SPS).

Using qualitative evidence such as the quality of the production process and extensive static analysis, the regulators accepted that the system was adequately safe based on this revised figure.<sup>2</sup> Some time later, and following the licensing of the reactor for operation, the PPS software was subjected to extensive statistically representative operational testing. This *direct* evaluation of its reliability supported the claim of  $10^{-3}$  *pdf* at a high-confidence level [16].

After the licensing of Sizewell B, the UK’s Advisory Committee on the Safety of Nuclear Installations (ACSNI) set up a Study Group on the Safety of Operational Computer Systems, chaired by one of the authors of this paper. Among the recommendations to the UK’s Health and Safety Executive (HSE) in the final published version of the report [17] was the following:

Confidence in assessments of software-based systems is usually less than for more conventionally engineered systems. We believe that attention should be given to incorporating formally in licensees’ and regulatory guidance a recognition of the importance of the level of confidence that can be placed in assessments of risk within the concept of an “adequate” safety case. What is needed is to clarify and define the notion of “adequacy,” such that it can be used to guide and justify decisions as to the required extent of activities that will establish the level of confidence that can be placed in a risk assessment.

During the Study Group’s discussions, it was suggested that the UK principle of As Low As Reasonably Practicable (ALARP)—referring to the required safety level (such as *pdf*)—should be accompanied by a similar one concerning confidence in that level having been achieved: “As Confident As Reasonably Practicable” (ACARP). At the time of writing, this suggestion of a formal demonstration of confidence has not been taken up.

However, the experiences from Sizewell and subsequent assessments have been codified in the UK nuclear industry’s reissued Safety Assessment Principles [18]. These explicitly require confidence building:

361 Independent “confidence-building” should provide an independent and thorough assessment of a safety system’s fitness for purpose. This comprises the following elements:

a) Complete and preferably diverse checking of the finally validated production software by a team that is independent of the systems suppliers, including:

- independent product checking providing a searching analysis of the product;
- independent checking of the design and production process, including activities needed to confirm the realization of the design intention; and

b) Independent assessment of the test program, covering the full scope of test activities.

362 Should weaknesses be identified in the production process, compensating measures should be applied to address these. The type of compensating measures will

2. This summary simplifies the detailed argument that takes into account the frequency of the different initiating events that the SPS and PPS protect against, and the scope of the PPS and SPS safety functions. The SPS is simpler in both the technology it uses and also in the scope of the functions it performs.

depend on, and should be targeted at, the specific weaknesses found.

Standards are generally silent on the question of confidence. For example, IEC61508 [19] has nothing to say about the confidence that can be placed in the failure probability levels (or failure rates) associated with Safety Integrity Levels (SILs). While more extensive and demanding evidence is needed to support the higher level SILs, there is no guidance on how much evidential support is needed to provide a particular confidence that a system lies in a certain SIL.

On the other hand, over 10 years ago UK Def Stan 00-56 [20] informally acknowledged the importance of confidence—for example, it recommended the use of a diverse two-legged argument to increase confidence in a dependability claim—but, again, it contained no guidance on issues concerning “how much” confidence can be claimed in particular instances. More recently, Issue 4 of the Def Stan [7] explicitly discusses the role of confidence and provides some guidance, albeit *qualitative*, on how to interpret high, medium, and low levels of confidence.

The need to address confidence explicitly in the HSE safety assessment principles, and the experience with the discussions about the PPS reliability (where the notion of confidence had been treated rather informally), suggest there may be advantages in exploring more formal—and ideally quantitative—models of confidence. These more formal approaches could provide a semantics for understanding and communicating “confidence” and provide a rigorous framework for negotiation during the licensing process.

An important goal of such a formalism would be to provide a clear notion of *how* confident an assessor is, or needs to be. In the Sizewell example, there were no clear answers to questions of the following kind:

- How confident was the assessor in the eventually accepted  $10^{-3}$  for the *pdf* of the PPS?
- How confident did the regulator *need* to be so as to “sign off” on this part of the safety case?
- How confident was the assessor in the original requirement of  $10^{-4}$  and how much did this confidence fall short of what was needed?

In order that an assessor’s epistemic doubt be included in the overall risk assessment, it is necessary that these questions be answered quantitatively in terms of the assessor’s subjective probabilities.

In the Sizewell example, it was also not clear how a *pdf* level, and the professed confidence in that level was *used*:

- If the assessor or regulator were “sufficiently” confident in  $10^{-3}$ , how would this number be used?
- Does “sufficiently confident” mean “I can treat the number as if it were true”?
- If, instead, “sufficiently confident” means something like 99 percent confident, then how is the residual 1 percent (i.e., the chance that the system is worse than the  $10^{-3}$  claim) treated?

At one stage, there seemed to be reasoning along the following lines: “We are reasonably confident that the *pdf* is better than  $10^{-4}$ ; to be on the safe side, however, we shall only claim  $10^{-3}$ , and this is so conservative that we can treat this figure as the true *pdf* in our calculations for the wider system (plant) safety case.” In this paper, we investigate whether this

kind of reasoning can ever be justified, and if so whether the resulting numbers can make it a useful approach.

It was interesting in the case of the Sizewell PPS that the numbers involved were rather modest. It seemed possible, in principle, for quite high confidence to be placed in these required levels of reliability. This contrasts with other industries where the required levels seem so demanding that it will never be feasible to assert high confidence in them convincingly [21], [22]. An obvious example concerns the controversial requirement of  $10^{-9}$  probability of failure per hour for particular flight-critical avionics systems in commercial airplanes: How much confidence in such a claim should a regulator place, based, for example, upon evidence of adherence to the guidelines in [23]? This is far from the most extreme example we have seen. Some railway signaling applications apparently require failure rates no worse than  $10^{-12}$  per hour [24].

Coming now to a safety case for a wider system—nuclear plant, commercial aircraft type—the top level claim for this system might be expressed, for example, as a probability of (safety related) failure on demand, or failure rate. This claim will, in turn, depend upon claims made at lower levels about subsystem functions: e.g., *pdf* of a protection system, e.g., failure rate of a flight control system. If we knew the values of these subsystem parameters with certainty, then in principle we could decide whether the claim required of the subsystem by the wider safety case had been satisfied. If, on the other hand, these parameters are not known with certainty, as seems likely, then these uncertainties need to be propagated through the safety case, and the reasoning becomes more difficult. In the remainder of the paper, it is this problem that we address when the claims at subsystem level concern *software*. We are not aware that such problems have been addressed previously in the software engineering literature.

## 2 STATEMENT OF PROBLEM, AND A CONSERVATIVE SOLUTION

As will be clear from the informal discussion above, human judgment inevitably forms an important element of any assessment of confidence (or its complement, doubt) when this arises from epistemic uncertainty. If, as we believe, confidence should be expressed probabilistically, the appropriate calculus of probability is a subjective Bayesian one.

The first problem in any Bayesian analysis is to obtain the prior beliefs of the expert. Consider an example in which a *pdf* is the subject of the dependability claim. This *pdf* can be regarded as an unknown number that characterizes the aleatory uncertainty discussed above. In principle, we could estimate this number to any degree of accuracy if we were in the fortunate position of being able to generate unlimited numbers of statistically representative test cases and we had a perfect oracle to decide whether each test case had been executed correctly. In practice, of course, we are never in this position: Instead, there is uncertainty about the value of the *pdf*. This is the epistemic uncertainty discussed above, arising from imperfect knowledge, etc. This uncertainty about the true value of this *pdf* requires it to be treated as a random variable,  $P$ , so that confidence is expressed as a probability. Thus, the expert may believe a priori that

$$\text{Prob}(P \leq y) = 1 - x \quad (1)$$

expressing his confidence,  $1 - x$ , that the *pdf* is smaller than  $y$ . If the expert were able to tell us the values of  $x$  corresponding to all possible values of  $y$ , we would have a distribution, say  $F$  (with probability density function  $f$ ), for the random variable  $P$ . This would describe the expert's complete (epistemic) a priori uncertainty about the value of the *pdf*. In fact, it is well known that experts find it hard to describe their complete uncertainty in this way: It is even hard to elicit just one or two  $(y, x)$  pairs.

The second problem concerns how we would use the information even if we knew  $f$  completely. Typically, such a claim (and its associated confidence) would be only one of several forming a dependability case. For example, this claim might concern only one subsystem among many others, or one among several functions of a wider system about which the top-level claim is being made. Propagating uncertainty about these many subsystem dependability claims (or dependability claims about many functions) through such complex cases can be difficult or even impossible.

A very informal solution to this problem that we have seen uses the following reasoning: "I wish to claim that the *pdf* of this component (or this function) is better than  $10^{-3}$ . I will attempt to collect sufficient evidence to be able to make a *much stronger* claim, e.g., *pdf* is smaller than  $10^{-5}$ , with high confidence. I will then conclude, because of my high confidence in this stronger claim, that the weaker claim is *conservative* (i.e., I am certain that the true *pdf* is better than this claim). I will then plug this conservative value into my calculation for the overall dependability of the wider system. I am confident that if I do this for all subsystems, my calculated claim for the *system* will be conservative."

Is such reasoning ever justified? There is an attractive conservatism in the approach. If the evidence is strong enough to replace the numbers in the previous paragraph by ones representing even stronger claims at even higher confidence, surely (it might be reasoned) eventually the expert will allow the modest claim of  $10^{-3}$  to be treated as if it were true?

In what follows, we show that such an approach can be placed on a formal footing. But it turns out that the conservatism in the approach can be *very* unforgiving, at least until a priori beliefs are supplemented by extensive evidence of failure-free working.

### 2.1 Result Based Only on Prior Beliefs

We start with the very simple situation where the expert has only a priori beliefs about the *pdf*.<sup>3</sup> In fact, he is only willing—or able—to express the beliefs represented by (1) above for a single  $(y, x)$  pair. In other words, we only know one point on his belief-distribution  $f$ .

If we had the complete distribution, then the quantity of interest here is the expert's subjective probability that there is failure on a randomly chosen demand

3. But note that such beliefs may arise from *informally* taking account of real evidence. The point here is that the expert is only prepared to tell us the beliefs expressed as a (claim, confidence/doubt) pair, but not the reasons for his holding such beliefs. We shall later consider the case where, following the expression of these a priori beliefs, the expert obtains some evidence from operational testing and uses this to modify his beliefs, using Bayes' theorem.

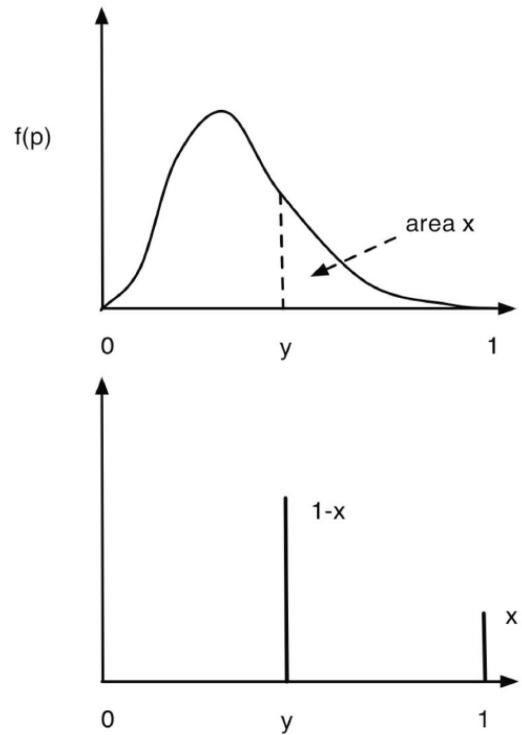


Fig. 1. A typical distribution for an expert's belief, and the most pessimistic distribution that satisfies the expert's  $(y, x)$  belief.

$$\begin{aligned} &\text{Prob (failure on randomly selected demand)} \\ &= \int_0^1 p \cdot f(p) dp = E(p) \end{aligned} \tag{2}$$

by the formula for total probability. This is, for example, the number that the expert might be prepared to "plug in" to a wider safety case: It takes account of the expert's complete aleatory and epistemic uncertainty.

At the top of Fig. 1 is a typical distribution for an expert's belief. In reality, an expert is unlikely to be able to express the infinitely many probabilities implicit in this figure. Instead, he may only be willing to tell us about one point on the distribution: represented here by  $y$ . Below is the *most pessimistic* of all possible distributions,  $f(p)$ , that satisfy the expert's  $(y, x)$  belief. It is obtained by placing the probability masses associated with the intervals  $(0, y)$ ,  $(y, 1)$  at the extreme right of the intervals. Note that here the bars represent probability mass in contrast to the probability density function in the upper figure.

The lower diagram in Fig. 1 can easily be seen to represent the "most pessimistic" set of beliefs—i.e., distribution  $f(p)$ —that satisfies the expert's professed belief, (1), because it is the distribution that maximizes (2), giving

$$\begin{aligned} &\text{Prob (failure on randomly selected demand)} = \int_0^1 p \cdot f(p) dp \\ &= \int_0^y p \cdot f(p) dp + \int_y^1 p \cdot f(p) dp < y(1 - x) + x \\ &= x + y - xy = y^*, \text{ say.} \end{aligned} \tag{3}$$

In other words, if the expert is prepared to accept a claim  $y$  with confidence  $1 - x$ , as (1) asserts, then (3) shows that he must believe the probability of failure on a randomly selected demand is smaller than  $y^* = x + y - xy$ . That is, he can treat  $y^*$  as the true probability of failure on demand—for example, in a wider safety case—and be assured that this is a conservative number.

Unfortunately, it is easy to see that this approach is *very* conservative when only a priori beliefs are considered, as here. For example, for  $10^{-3}$  to be an upper bound on the expert's (subjective) probability of failure on demand, he would need to have 99.91 percent confidence that the random variable, *pdf*, is smaller than  $10^{-4}$ . The problem lies in the exact symmetry of the roles of  $x$  and  $y$  in (3): Any claim,  $y^*$ , he makes with certainty must be numerically greater than the *doubt*,  $x$ , in the stronger claim,  $y$ . Note that this is true regardless of the value of  $y$ , but in realistic situations,  $x$  will usually be much larger than  $y$ .

This is, of course, disappointing and means that the result is unlikely to be of practical interest. When evidence of successful operation is available, however, the picture changes for the better.

## 2.2 Result Based on Evidence of Failure-Free Working

It is interesting to ask what is the pessimistic (but attainable) bound for “probability of failure on a randomly selected demand” when some failure-free operation<sup>4</sup> has been seen (or, for that matter, some operation that might have included some failures<sup>5</sup>).

When  $n$  failure-free demands have been observed, the expert's beliefs about  $P$  change from his prior belief, represented by  $f(p)$ , via Bayes theorem: His conditional distribution becomes

$$f(p \mid n \text{ failure-free demands}) = \frac{(1-p)^n f(p)}{\int_0^1 (1-p)^n f(p) dp}. \quad (4)$$

The expert's posterior probability of failure on demand is just the mean of this:

$$\begin{aligned} \text{Prob (system fails on randomly selected demand} \\ \text{ } n \text{ failure-free demands)} &= \frac{\int_0^1 p(1-p)^n f(p) dp}{\int_0^1 (1-p)^n f(p) dp} \\ &= E(p \mid n \text{ failure-free demands}). \end{aligned} \quad (5)$$

Clearly, the “most pessimistic” two-point distribution above no longer applies—there cannot be positive probability mass at 1 following the observation of failure-free demands. So the question is: What is the most pessimistic  $f(p)$ , still satisfying (1), which maximizes (5)?

In fact, somewhat surprisingly, it can be shown that this is once again a two-point distribution (see the Appendix for proof). As before, it has probability mass  $(1-x)$  concentrated at  $y$  and probability mass  $x$  concentrated at  $z$ , where the value of  $z$  is chosen to maximize the posterior mean of  $P$ , which is, by substitution in (5):

4. Such operation must, of course, be statistically representative of operational use, and the oracle used to determine that all demands are successful must be perfect.

5. But which are not *all* failures because then the two-point distribution above will be the worst-case one, with probability mass at 1.

TABLE 1  
Examples of the Worst-Case True Probabilities of Failure,  
Based on an Expert's Prior Beliefs about a Claim  
of  $y = 0.5 \times 10^{-3}$

$n \backslash (1-x)$	0.90	0.95	0.99
0	0.10045	0.050475	0.010495
1	0.026821	0.013316	0.003011
5	0.007626	0.003951	0.001173
10	0.004235	0.002307	0.000852
30	0.001787	0.001122	0.000621
50	0.001278	0.000876	0.000573
100	0.000891	0.000689	0.000537
500	0.000578	0.000538	0.000507
1000	0.000539	0.000519	0.000504

$$\frac{y(1-y)^n(1-x) + z(1-z)^n x}{(1-y)^n(1-x) + (1-z)^n x} = h(z), \text{ say.} \quad (6)$$

The value of  $z$  corresponding to the most pessimistic two-point  $(y, z)$  distribution is the one in  $(0, 1)$  satisfying  $h'(z) = 0$ , i.e., satisfying

$$\frac{(1-z)^{n+1} x}{(n+1)z - ny - 1} = (1-y)^n(1-x) \quad (7)$$

for  $n > 0$  (for  $n = 0$ ,  $h'(z) = x > 0$ ).

Using this distribution in (5), we obtain the value of the probability of failure on a randomly selected demand that the expert can treat as “true” (e.g., for a wider safety case), and know that it is conservative (but attainable). It is easy to see from (6) that this “true” *pdf* converges to  $y$  as  $n$  goes to infinity (with  $z$  converging to  $y$ ) since  $(1-z) < (1-y)$ .

Table 1 shows some examples, when the expert expresses his prior beliefs in terms of a claim of  $0.5 \times 10^{-3}$ . Thus, when he has a prior confidence of 99 percent that the *pdf* is smaller than  $0.5 \times 10^{-3}$ , he can only claim 0.010495 with certainty before seeing any evidence of failure-free working. Such unforgiving results from Section 2.1, however, quickly become more useful as evidence of failure-free operation is gathered: With only 50 failure-free demands and the same prior belief, he can be certain the probability of failure on a randomly chosen demand is better than 0.000573. Compare this with  $0.0005 = 0.5 \times 10^{-3}$ —his original claim in which he had a prior confidence of 0.99. As the evidence of failure-free working gets larger, the expert becomes closer and closer to certain that the original *pdf* claim is true (a priori, remember, he was only 99 percent confident in this claim). But the expert can never be certain of a *stronger* claim that his original  $0.5 \times 10^{-3}$ , however much evidence he sees of perfect working.

## 2.3 Result When the Expert Believes It Is Possible That There Are No Faults

A problem with the previous result is that no matter how much evidence of perfect working the expert sees, his

worst-case probability of failure for a randomly selected demand cannot be better than  $y$ : It is easy to see that the expression  $h(z)$  in (6) goes to  $y$  as  $n$  goes to infinity.

The reason lies in the extreme conservatism of placing all the expert's belief about the *pdf* taking values to the left of  $y$  exactly at  $y$ . As  $n$  increases, the expert's beliefs change as a result of two effects: The second point of support for the expert's conservative belief,  $z$ , moves to the left and the probability mass at  $y$  increases (with a corresponding reduction of the mass at  $z$ ). In the limit, all of the the mass is concentrated at  $y$ , *but there is still no probability mass to the left of  $y$ .*

A real expert might regard this result as *too* conservative: Most of us would regard very many failure-free demands to be evidence of very low probability of failure on demand. We might believe that *any* probability of failure for a randomly selected demand, however small, could be accepted if a *sufficiently large* number of failure-free demands had been seen.<sup>6</sup>

As we shall see below, one way this can happen is the situation in which the expert is prepared to believe a priori in the possibility that the system is completely fault-free, however small his prior probability for this.

We proceed by modifying the previous expressions for the expert's prior beliefs as follows: The expert now believes, before seeing any evidence from the working system:

- $\text{Prob}(P = 0) = \alpha$ .
- For  $p > 0$ , the expert's beliefs are represented by an improper probability density function  $f(p)$ .<sup>7</sup> As before, he is only willing (or able) to tell us one point on this distribution:  $\text{Prob}(P \leq y \mid P > 0) = 1 - x - \alpha$ .

This formulation retains the former belief that  $\text{Prob}(P \leq y) = 1 - x$ , thus allowing a comparison with the earlier results.

The most pessimistic prior satisfying the expert's beliefs is now the one where (generalizing the lower distribution in Fig. 1) all of the the probability mass is concentrated at *three* points:

- $\text{Prob}(P = 0) = \alpha$ .
- $\text{Prob}(P = y) = 1 - x - \alpha$ .
- $\text{Prob}(P = 1) = x$ .

From this pessimistic prior, we have

$$\begin{aligned} & \text{Prob}(\text{failure on randomly selected demand}) \\ &= \int_0^1 p \cdot f(p) dp < x + y - xy - \alpha y = y^{**} \end{aligned} \quad (8)$$

cf. (3). Once again, the expert can treat  $y^{**}$  as the true probability of failure on demand—for example, in a wider safety case—and be assured that this is a conservative number. As before, this bound, based solely on prior beliefs, is very conservative, so it is again interesting to see what happens when  $n$  failure-free demands have been seen.

The expert's posterior beliefs are a mixed distribution again, with some probability mass at the origin, and an

improper continuous probability density function when  $p > 0$ :

$$\begin{aligned} p_0(n) &\equiv \text{Prob}(P = 0 \mid n \text{ failure-free demands}) \\ &= \frac{\text{Prob}(n \text{ failure-free demands} \wedge P = 0)}{\text{Prob}(n \text{ failure-free demands})} \\ &= \frac{\alpha}{\int_0^1 (1-p)^n f(p) dp + \alpha} \end{aligned} \quad (9)$$

and

$$\begin{aligned} & f(p \mid n \text{ failure-free demands}) \\ &= \frac{(1-p)^n f(p)}{\int_0^1 (1-p)^n f(p) dp + \alpha}, \quad p > 0. \end{aligned} \quad (10)$$

Again, this is an improper density function—it does not integrate to unity. Instead,

$$\begin{aligned} & \int_0^1 f(p \mid n \text{ failure-free demands}) dp \\ &= 1 - \text{Prob}(P = 0 \mid n \text{ failure-free demands}). \end{aligned}$$

The expert's posterior probability of failure on demand is

$$\begin{aligned} & \text{Prob}(\text{system fails on randomly selected demand} \mid \\ & n \text{ failure-free demands}) = \frac{\int_0^1 p(1-p)^n f(p) dp}{\int_0^1 (1-p)^n f(p) dp + \alpha}. \end{aligned} \quad (11)$$

As before, it can be shown that the most pessimistic improper density,  $f(p)$ , is a two-point distribution having probability mass  $(1 - x - \alpha)$  concentrated at  $y$  and probability mass  $x$  concentrated at  $z$ , where the value of  $z$  is chosen to maximize the posterior mean of  $p$ , which is, by substitution in (11),

$$\frac{y(1-y)^n(1-x-\alpha) + z(1-z)^n x}{(1-y)^n(1-x-\alpha) + (1-z)^n x + \alpha}. \quad (12)$$

The conservative posterior probability that the system is fault free is obtained by substituting the most pessimistic prior  $f(p)$  into the expression (9):

$$p_0(n) = \frac{\alpha}{(1-y)^n(1-x-\alpha) + (1-z)^n x + \alpha}. \quad (13)$$

It is easy to see that this increases as  $n$  increases, and  $p_0(n) \rightarrow 1$  as  $n \rightarrow \infty$ . Thus, confidence in fault freeness can be made arbitrarily close to certainty by the observation of a sufficiently large number of failure-free demands, however small the expert's a priori confidence in fault freeness.

As before,  $z \rightarrow y$  as  $n \rightarrow \infty$ . Tables 2, 3 and 4 give some feel for the way in which posterior beliefs—both for the “plug-in” probability of failure on a randomly selected demand, and for the probability of fault freeness—depend upon the prior beliefs and the amount of failure-free working that has been seen.

For example, in all cases here the expert will be able to treat the original claim—0.0005—as true after only a modest number of failure-free demands. He will be able to treat as true, a claim that is an order of magnitude better than this if he has strong enough a priori belief in perfection ( $\alpha = 0.9$  in Table 3). While such a belief might seem unreasonably

6. Assuming, of course, that the oracle can be trusted completely, and the operational profile accurately represents real use.

7. That is  $\int_0^1 f(p) dp = 1 - \alpha$ .

**TABLE 2**  
Examples of the Worst Case True Probabilities of Failure, Based on an Expert's Prior Beliefs about a Claim of  $y = 0.5 \times 10^{-3}$ , with  $\alpha = 0.1$

$1-x$ $n$	0.90		0.95		0.99	
	Mean	$p_0(n)$	Mean	$p_0(n)$	Mean	$p_0(n)$
0	0.1004	0.1	0.050425	0.1	0.010445	0.1
1	0.026767	0.105456	0.013264	0.102644	0.002961	0.100549
5	0.007571	0.106759	0.003899	0.103350	0.001123	0.100830
10	0.004180	0.107183	0.002255	0.103669	0.000802	0.101073
30	0.001731	0.108274	0.001069	0.104663	0.000570	0.101997
50	0.001221	0.109266	0.000822	0.105615	0.000521	0.102919
100	0.000833	0.111733	0.000634	0.108005	0.000484	0.105251
500	0.000498	0.135607	0.000467	0.129948	0.000443	0.125860
1000	0.000441	0.168920	0.000433	0.161356	0.000423	0.154890

Here, "Mean" is the worst-case probability of failure on demand that the expert can treat as true; " $p_0(n)$ " is the expert's posterior probability that the system is fault free. The numbers below the horizontal line in the table correspond to means that are smaller than the original claim of  $y = 0.5 \times 10^{-3}$ , i.e., the expert can treat this conservatively as true.

strong, it should be remembered that all of these results correspond to the same prior belief,  $\text{Prob}(P \leq y) = 1 - x$ : They differ only in how this is partitioned into beliefs about  $P = 0$  and  $0 < P \leq y$ .

### 3 DISCUSSION

We have provided a formalism to support the kind of argument that has sometimes been used informally in real safety cases. That is, an expert can treat a claim about probability of failure on demand as true if he has sufficient confidence—albeit not certainty—in the truth of a stronger claim and he can be sure that this "modest" claim will be conservative. The value of such an approach, of course, is

**TABLE 3**  
As Table 2, but with  $\alpha = 0.5$

$1-x$ $n$	0.90		0.95		0.99	
	Mean	$p_0(n)$	Mean	$p_0(n)$	Mean	$p_0(n)$
0	0.1002	0.5	0.050225	0.5	0.010245	0.5
1	0.026550	0.527163	0.013056	0.513111	0.002759	0.502643
5	0.007350	0.533201	0.003689	0.516208	0.000921	0.503638
10	0.003958	0.534725	0.002044	0.517255	0.000599	0.504344
30	0.001508	0.537761	0.000858	0.52001	0.000367	0.506893
50	0.000997	0.540268	0.000610	0.522518	0.000318	0.509396
100	0.000607	0.546281	0.000420	0.528668	0.000278	0.515627
500	0.000256	0.605383	0.000238	0.583725	0.000222	0.566232
1000	0.000186	0.667187	0.000189	0.643364	0.000189	0.622626

**TABLE 4**  
As Tables 2, 3, but with  $\alpha = 0.9$

$1-x$ $n$	0.90		0.95		0.99	
	Mean	$p_0(n)$	Mean	$p_0(n)$	Mean	$p_0(n)$
0	0.1	0.9	0.050025	0.9	0.010045	0.9
1	0.026334	0.948683	0.012849	0.923405	0.002558	0.904575
5	0.007129	0.958696	0.003479	0.928197	0.000719	0.905633
10	0.003737	0.960371	0.001834	0.929102	0.000398	0.905988
30	0.001288	0.961564	0.000649	0.930145	0.000166	0.906910
50	0.000778	0.961811	0.000402	0.930741	0.000118	0.907742
100	0.000391	0.961998	0.000214	0.932010	0.000080	0.909755
500	0.000079	0.962148	0.000051	0.950834	0.000042	0.926374
1000	0.000039	0.962167	0.000027	0.962996	0.000032	0.937030

Note that the result in the first two columns corresponds to  $1 - x = \alpha = 0.9$ . In this case, the expert's prior beliefs have no probability density between 0 and  $y$ , so the most pessimistic prior has probability mass on only two points,  $\text{Prob}(P = 0) = 0.9$  and  $\text{Prob}(P = 1) = 0.1$  so that the a priori mean is 0.1, as shown in the first cell. The higher horizontal lines here are as in the previous figures. Beneath the lower horizontal lines, the expert can conservatively treat as true, a claim that the pfd is no worse than  $0.5 \times 10^{-4}$ , i.e., an order of magnitude better than the original claim (about which he had a priori doubt).

that this conservative pfd value can simply be "plugged in" to a wider safety case, and the expert can know that the effect on any claims made at this higher level will be conservative.

This approach is much simpler and more practical than taking complete account of the uncertainty about a pfd value for two reasons:

- It is well known that experts find it difficult to describe their beliefs in terms of a complete distribution, but they may be able to probabilistically express their confidence that a variable (e.g., a pfd) is smaller than a given number (i.e., a single percentage point on the distribution of their beliefs).
- Even if a complete distribution were available, it would be very difficult to propagate this through a wider safety case (e.g., where the reliability of the wider system is a function of the reliabilities of many other subsystems). Propagating known-to-be-conservative numbers, in contrast, is in principle simple.

Not surprisingly, when based upon a priori beliefs alone, as in Section 2.1, such an approach is very conservative; in fact, it is too conservative to have practical usefulness. But when the expert begins to see evidence of failure-free working (as in Section 2.2), this conservatism lessens, and it seems that the results can be useful.

However, as we note, the conservative claim is bounded by the value of  $y$  in the expert's original statement of belief,  $(y, x)$ . Even with extensive evidence of perfect working, the best that can be claimed is  $y$ . It seems reasonable that a real expert would—at least after the fact, when confronted with extensive successful operation—find that this did not represent his expectations. Rather, most experts, we believe,

would come to believe that the *pdf* is smaller than *any*  $y^*$  for sufficiently large  $n$ , i.e.,  $y^* \rightarrow 0$  as  $n \rightarrow \infty$ .

The reason for the extreme conservatism is that we place all the probability mass lying to the left of  $y$  in the expert's a priori distribution  $f(p)$  upon the point  $y$  itself. The expert has said initially "all I can tell you about my prior beliefs is that the chance of the *pdf* being smaller than  $y$  is  $1 - x$ ." In fact, if specifically questioned about it, it is likely that he would be prepared to say something further along the lines of: "I cannot tell you anything further in detail about how my beliefs are distributed in the interval  $(0, y)$ , except that  $f(p)$  is nonzero at all points in this interval." In other words, our conservatism is *too* conservative to represent his beliefs about the *pdf* in the interval  $(0, y)$ .

Of course, this conservatism places a serious constraint on the usefulness of the results here. Imagine that, for a wider safety case, we need to claim a *pdf* no worse than  $y^*$  for the system under examination and that  $y^* < y$ . No matter how much evidence of successful operation he collects, the expert will not be able to make the  $y^*$  claim unless he is prepared to expand his expressed a priori beliefs beyond the  $(y, x)$  used in our analysis.

A theoretical way forward is for the expert to give a second point on the distribution of his prior belief distribution,  $f(p)$ —say  $(y^{**}, x^{**})$ , where  $y^{**} < y^*$ —essentially expressing belief about the interval  $(0, y)$  similarly to his earlier expression of belief about  $(0, 1)$ . It is then easy to extend the results in the earlier part of the paper to show that as the number of failure-free demands,  $n$ , increases, the conservative claim approaches the bound  $y^{**}$ . That is, for a sufficiently large  $n$ , the expert will be able to claim the required  $y^*$  ( $> y^{**}$ ).

The difficulty with this approach, of course, is that the expert has to be able to tell us his belief, expressed as a probability, that the *pdf* is smaller than  $y^{**}$ —i.e., he has to be able to quantify a *very small* confidence,  $1 - x^{**}$ . It is well known that experts are very poor at estimating the extreme tails of probability distributions.

Notice how the reasoning required here contrasts with that involved in the analysis of Section 2.3. Here, the expert believes there is probability mass at the origin and so is expressing a belief about *perfection*. He might plausibly reason something like this: "This system has very simple functionality, it has been designed very simply, and I have evidence of certain kinds of formal verification of its correctness, so I think there is a chance that they got it completely right." This is very different from reasoning that "I know this system is too complex to be correct, so I know it will eventually fail in operation, but I am reasonably confident that the *pdf* is extremely small." The two statements are very different in kind and support for them comes from very different evidence. We think that real experts would be more comfortable with the former than with the latter.

The work reported here represents only the beginnings of a practical probabilistic calculus of confidence for dependability cases—clearly much further work is needed. The problems are both theoretical and practical. Theoretical issues concern the representation and propagation of confidence through complex cases, which typically involve

many disparate sources of doubt. Practical issues concern doing this with different, often incomplete, evidence sources.

For example, in this paper, we have only considered the situation in which interest centers upon the probability of failure on a randomly selected demand. Imagine, instead, we were interested in the probability of surviving  $m$  future demands (say, the number of demands expected in the system's lifetime). It would be incorrect simply to use the conservative bound, say  $y^*$ , obtained as above and estimate this probability using  $(1 - y^*)^m$ . Instead, we would need to find the prior that produces the most conservative value of  $E((1 - P)^m)$ . Similar comments apply to other dependability measures: The point here is that a prior that is conservative for one measure will not generally be conservative for another.

Other issues and questions for future study include the following:

- Does the approach generalize to claims based on continuous measures, e.g., failure rates?
- Can the results be generalized to the multiattribute case, where claims concern more than one measure, e.g., (*pdf*, availability)?
- Can other kinds of evidence, of the kinds available for realistic safety cases, be used in this kind of analysis?

## APPENDIX

### STATEMENT

Let  $P$  be the system *pdf* treated as a random variable with density  $f(p)$ .

Here, we show that

$$E(P \mid n \text{ failure free demands}) = 1 - \frac{\int_0^1 (1-p)^{n+1} f(p) dp}{\int_0^1 (1-p)^n f(p) dp} \quad (1)$$

$$\leq 1 - \frac{(1-p_1)^{n+1}(1-x) + (1-p_2)^{n+1}x}{(1-p_1)^n(1-x) + (1-p_2)^n x},$$

where

$$0 \leq p_1 \leq y \leq p_2 \leq 1$$

$$\int_0^y f(p) dp = 1 - x,$$

and the bound (1) is reached with the two-point prior probability distribution of  $P$ :

$$\text{Prob}(P = p_1) = 1 - x;$$

$$\text{Prob}(P = p_2) = x.$$

**Lemma.** *If  $q$  is a positive random variable and  $n$  is a positive integer, then*

$$[E(q^{n+1})]^{\frac{1}{n+1}} \geq [E(q^n)]^{\frac{1}{n}}.$$

**Proof.** If  $x \geq 0$  and  $a \geq 1$ , the function  $f(x) = x^a$  is convex, so, by Jensen's inequality,

$$E(x^a) \geq (E(x))^a. \quad (2)$$

Substituting  $x = q^n$  and  $a = \frac{n+1}{n}$  into (2):

$$E(q^{n+1}) \geq [E(q^n)]^{\frac{n+1}{n}},$$

which implies

$$[E(q^{n+1})]^{\frac{1}{n+1}} \geq [E(q^n)]^{\frac{1}{n}}.$$

□

**Proof of the Statement.** Let us introduce four (unknown) values  $p_1, p_2, p_3, p_4$ :

$$\begin{aligned} p_1 &= 1 - \left( \frac{\int_0^y (1-p)^{n+1} f(p) dp}{1-x} \right)^{\frac{1}{n+1}}, \\ p_2 &= 1 - \left( \frac{\int_y^1 (1-p)^{n+1} f(p) dp}{x} \right)^{\frac{1}{n+1}}, \\ p_3 &= 1 - \left( \frac{\int_0^y (1-p)^n f(p) dp}{1-x} \right)^{\frac{1}{n}}, \\ p_4 &= 1 - \left( \frac{\int_y^1 (1-p)^n f(p) dp}{x} \right)^{\frac{1}{n}}. \end{aligned}$$

Obviously,

$$\begin{aligned} 0 &\leq p_1, p_3 \leq y, \\ y &\leq p_2, p_4 \leq 1. \end{aligned}$$

In accordance with the lemma

$$p_1 \leq p_3, \quad (3)$$

$$p_2 \leq p_4 \quad (4)$$

because

$$\begin{aligned} 1 - p_1 &= (E((1-P)^{n+1} | P \leq y))^{\frac{1}{n+1}}, \\ 1 - p_3 &= (E((1-P)^n | P \leq y))^{\frac{1}{n}}, \\ 1 - p_2 &= (E((1-P)^{n+1} | P > y))^{\frac{1}{n+1}}, \\ 1 - p_4 &= (E((1-P)^n | P > y))^{\frac{1}{n}}. \end{aligned}$$

We can now use the values  $p_1, p_2, p_3, p_4$  to write down an expression for  $E(P | n \text{ successful runs})$

$$\begin{aligned} E(P | n \text{ successful runs}) &= 1 - \frac{\int_0^y (1-p)^{n+1} f(p) dp}{\int_0^1 (1-p)^n f(p) dp} \\ &= 1 - \frac{\int_0^y (1-p)^{n+1} f(p) dp + \int_y^1 (1-p)^{n+1} f(p) dp}{\int_0^y (1-p)^n f(p) dp + \int_y^1 (1-p)^n f(p) dp} \quad (5) \\ &= 1 - \frac{(1-p_1)^{n+1}(1-x) + (1-p_2)^{n+1}x}{(1-p_3)^n(1-x) + (1-p_4)^n x}. \end{aligned}$$

Applying (3) and (4) to (5), we finally obtain the following upper bound:

$$\begin{aligned} E(P | n \text{ successful runs}) \\ \leq 1 - \frac{(1-p_1)^{n+1}(1-x) + (1-p_2)^{n+1}x}{(1-p_1)^n(1-x) + (1-p_2)^n x}, \quad (6) \end{aligned}$$

and the bound (6) is obviously reached when one chooses the two-point prior distribution of  $P$ :

$$Prob(P = p_1) = 1 - x;$$

$$Prob(P = p_2) = x;$$

$$0 \leq p_1 \leq y \leq p_2 \leq 1.$$

□

**Comment.** The unknown values  $p_1$  and  $p_2$  are found as a solution of the two-dimensional optimization problem

$$\frac{(1-p_1)^{n+1}(1-x) + (1-p_2)^{n+1}x}{(1-p_1)^n(1-x) + (1-p_2)^n x} \rightarrow \min$$

subject to constraints

$$\begin{aligned} 0 &\leq p_1 \leq y; \\ y &\leq p_2 \leq 1. \end{aligned}$$

In general,  $p_1$  and  $p_2$  may differ from  $y$  and 1.

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